

A New Algebraic Method to Search Irreducible Polynomials Using Decimal Equivalents of Polynomials over Galois Field GF(p^q)

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Abstract. Irreducible polynomials play an important role till now, in construction of 8-bit S-Boxes in ciphers. The 8-bit S-Box of Advanced Encryption Standard is a list of decimal equivalents of Multiplicative Inverses (MI) of all the elemental polynomials of a monic irreducible polynomial over Galois Field GF(2⁸) [1]. In this paper a new method to search monic Irreducible Polynomials (IPs) over Galois fields GF(p^q) has been introduced. Here the decimal equivalents of each monic elemental polynomial (ep), two at a time, are split into the p-nary coefficients of each term, of those two monic elemental polynomials. From those coefficients the p-nary coefficients of the resultant monic basic polynomials (BP) have been obtained. The decimal equivalents of resultant basic polynomials with p-nary coefficients are treated as decimal equivalents of the monic reducible polynomials, since monic reducible polynomials must have two monic elemental polynomials as its factor. The decimal equivalents of polynomials belonging to the list of reducible polynomials are cancelled leaving behind the monic irreducible polynomials. A non-monic irreducible polynomial is computed by multiplying a monic irreducible polynomial by α where $\alpha \in GF(p^q)$ and assumes values from 2 to (p-1).

General Terms: Algorithms, Irreducible polynomial.

Keywords: Finite field, Galois field, Irreducible polynomials, Decimal Equivalents.

1. Introduction:

A basic polynomial BP(x) over finite field or Galois Field GF(p^q) is expressed as,

$$BP(x) = a_q x^q + a_{q-1} x^{q-1} + \dots + a_1 x + a_0.$$

B(x) has (q+1) terms, where a_q is non-zero and is termed as the leading coefficient [2]. A polynomial is monic if a_q is unity, else it is non-monic. The GF(p^q) have $(p^q - p)$ elemental polynomials ep(x) ranging from p to $(p^q - 1)$ each of whose representation involves q terms with leading coefficient a_{q-1} . The expression of ep(x) is written as,

$$ep(x) = a_{q-1} x^{q-1} + \dots + a_1 x + a_0, \text{ where } a_1 \text{ to } a_{q-1} \text{ are not simultaneously zero.}$$

Many of BP(x), which has an elemental polynomial as a factor under GF(p^q), are termed as reducible. Those of the BP(x) that have no factors are termed as irreducible polynomials IP(x) [3][4] and is expressed as,

$$IP(x) = a_q x^q + a_{q-1} x^{q-1} + \dots + a_1 x + a_0, \text{ where } a_q \neq 0.$$

In Galois field GF(p^q), the decimal equivalents of the basic polynomials of extension q vary from p^q to $(p^{q+1} - 1)$ while the elemental polynomials are those with decimal equivalents varying from p to $(p^q - 1)$. Some of the monic basic polynomials are irreducible, since it has no monic elemental polynomial as a factor. The method in this paper is to look for the decimal equivalents of the reducible polynomials with multiplication, addition and modulus, of the p-nary coefficients of each term of each two monic elemental polynomials to obtain the decimal equivalent of the p-nary coefficients of each term of the resultant monic basic polynomial. The resultant monic basic polynomials are termed as reducible polynomials, since it is the product of two monic elemental polynomials. The polynomials belonging to the list of reducible polynomials are cancelled leaving behind the monic irreducible polynomials. A non-monic irreducible polynomial is computed by multiplying a monic irreducible polynomial by α where $\alpha \in GF(p)$ and assumes values from 2 to (p-1). In literatures, to the best knowledge of the present authors, there is no

mention of a paper in which the composite polynomial method is translated into an algorithm and in turn into a computer program.

Since 1967 researchers took algorithmic initiatives, followed by computational time-complexity analysis, to factorize basic polynomials on $GF(p^q)$ with a view to get irreducible polynomials, many of them are probabilistic [5][6][7][8] in nature and few of them are deterministic [9][10]. One may note that the deterministic algorithms are able to find all irreducible polynomials, while the probabilistic ones are able to find many, but not all. The irreducible polynomial over $GF(2^8)$ was first used in cryptography for designing an invertible 8-bit S-Box of AES [11][12][13]. The technique involves finding all multiplicative inverses under an irreducible polynomial is available in [14][15][16][17].

For convenient understanding, the proposed algebraic method is presented in Sec. 2 for $p=7$ with $q=7$. The method can find all monic and non-monic irreducible polynomials $IP(x)$ over $GF(7^7)$. Sec. 3 is demonstrates the obtained results to show that the proposed searching algorithm is actually able to search for any extension of the Galois field with any prime of $GF(p^q)$, where $p= 3, 5, 7, \dots, 101, \dots, p$ and $q= 2, 3, 5, 7, \dots, 101, \dots, q$. In Sec.4 and 5, the conclusion of the paper and the references are illustrated. A sample list of the decimal equivalents of the monic irreducible polynomials over Galois Field $GF(7^7)$ is given in Appendix.

2 Algebraic method to find Irreducible Polynomials over $GF(p^q)$

The basic idea of the algebraic method is to split the decimal equivalents of each monic elemental polynomial of a monic Basic Polynomial, any two at a time, into p -nary coefficients of each term of those monic elemental polynomials. Then multiply the p -nary coefficients to obtain each coefficients of the term with equal degree of each term of monic basic polynomials. All the multiplied results are then added to obtain the decimal coefficients of each term of the resultant monic basic polynomial. The decimal coefficients of each term of resultant monic basic polynomial are then reduced to p -nary coefficients of each term of that polynomial. The decimal equivalents of resultant monic basic polynomials with p -nary coefficients of each term are the decimal equivalents of the monic reducible polynomials since it has two monic elemental polynomials as its factor. The polynomials belonging to the list of monic reducible polynomials are cancelled leaving behind the monic irreducible polynomials. A non-monic irreducible polynomial is computed by multiplying a monic irreducible polynomial by α where $\alpha \in GF(p)$ and assumes values from 2 to $(p-1)$. The algebraic method to find the monic Irreducible polynomial over $GF(7^7)$ is demonstrated in section 2.2 and the extension to any Galois Field $GF(p^q)$ is described in section 2.2. The general method to develop each block of the algorithm of the algebraic method is demonstrated in section 2.3. The pseudo code for the above algebraic method is described in section 2.4.

2.1 Algebraic method to find Irreducible Polynomials over Galois Field $GF(7^7)$.

Here the interest is to find the monic irreducible polynomials over Galois Field or $GF(7^7)$.where $p=7$ is the prime field and $q=7$ is the extension of that prime field. Since the indices of multiplicand and multiplier are added to obtain the product. The extension $q=7$ can be demonstrated as a sum of two integers d_1 and d_2 , The degree of highest degree term present in elemental polynomials of $GF(7^7)$ is $(q-1) = 6$ to 1, since the polynomials with highest degree of term 0, are constant polynomials and they do not play any significant role here, so they are neglected. Hence the two set of monic elemental polynomials for which the multiplication is a monic basic polynomial where $p=7$, $q=7$, have the degree of highest degree terms d_1, d_2 where, $d_1=1,2,3$, and the corresponding values of d_2 are, 6,5,4. Number of coefficients in the monic basic polynomial $BP = (q+1) = (7+1) = 8$; they are defined as $BP_0, BP_1, BP_2, BP_3, BP_4, BP_5, BP_6, BP_7$, the value of the suffix also indicates the degree of the term of the monic basic polynomial. For monic polynomials $BP_7= 1$. Total number of blocks is the number of integers in d_1 or d_2 , i.e. 3 for this case.

Coefficients of each term in the 1st monic elemental polynomial EP⁰ where, d₁=1; are defined as EP₀⁰, EP₁⁰. Coefficients of each term in the 2nd monic elemental polynomial EP¹ where d₂=6; are defined as EP₀¹, EP₁¹, EP₂¹, EP₃¹, EP₄¹, EP₅¹, EP₆¹. The value in suffix also gives the degree of the term of the monic elemental polynomials. Now, the algebraic method is as follows,

1st block:

$$\begin{aligned} \text{BP}_0 &= (\text{EP}_0^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_1 &= (\text{EP}_0^0 * \text{EP}_1^1 + \text{EP}_1^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_2 &= (\text{EP}_0^0 * \text{EP}_2^1 + \text{EP}_1^0 * \text{EP}_1^1) \% 7. \\ \text{BP}_3 &= (\text{EP}_0^0 * \text{EP}_3^1 + \text{EP}_1^0 * \text{EP}_2^1) \% 7. \\ \text{BP}_4 &= (\text{EP}_0^0 * \text{EP}_4^1 + \text{EP}_1^0 * \text{EP}_3^1) \% 7. \\ \text{BP}_5 &= (\text{EP}_0^0 * \text{EP}_5^1 + \text{EP}_1^0 * \text{EP}_4^1) \% 7. \\ \text{BP}_6 &= (\text{EP}_0^0 * \text{EP}_6^1 + \text{EP}_1^0 * \text{EP}_5^1) \% 7. \\ \text{BP}_7 &= (\text{EP}_1^0 * \text{EP}_6^1) \% 7 = 1. \end{aligned}$$

Now the given basic monic polynomial is,

$$\text{BP}(x) = \text{BP}_7 x^7 + \text{BP}_6 x^6 + \text{BP}_5 x^5 + \text{BP}_4 x^4 + \text{BP}_3 x^3 + \text{BP}_2 x^2 + \text{BP}_1 x^1 + \text{BP}_0 x^0.$$

$$\text{Decm_eqv}(\text{BP}(x)) = \text{BP}_7 * 7^7 + \text{BP}_6 * 7^6 + \text{BP}_5 * 7^5 + \text{BP}_4 * 7^4 + \text{BP}_3 * 7^3 + \text{BP}_2 * 7^2 + \text{BP}_1 * 7^1 + \text{BP}_0 * 7^0.$$

Coefficients of each term in the 1st elemental monic polynomial EP⁰ where, d₁=2; are defined as EP₀⁰, EP₁⁰, EP₂⁰. Coefficients of each term in the 2nd elemental monic polynomial EP¹ where d₂=5; are defined as EP₀¹, EP₁¹, EP₂¹, EP₃¹, EP₄¹, EP₅¹. The value in suffix also gives the degree of the term of the monic elemental polynomials. Now, the algebraic method is as follows,

2nd block:

$$\begin{aligned} \text{BP}_0 &= (\text{EP}_0^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_1 &= (\text{EP}_0^0 * \text{EP}_1^1 + \text{EP}_1^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_2 &= (\text{EP}_0^0 * \text{EP}_2^1 + \text{EP}_1^0 * \text{EP}_1^1 + \text{EP}_2^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_3 &= (\text{EP}_0^0 * \text{EP}_3^1 + \text{EP}_1^0 * \text{EP}_2^1 + \text{EP}_2^0 * \text{EP}_1^1) \% 7. \\ \text{BP}_4 &= (\text{EP}_0^0 * \text{EP}_4^1 + \text{EP}_1^0 * \text{EP}_3^1 + \text{EP}_2^0 * \text{EP}_2^1) \% 7. \\ \text{BP}_5 &= (\text{EP}_0^0 * \text{EP}_5^1 + \text{EP}_1^0 * \text{EP}_4^1 + \text{EP}_2^0 * \text{EP}_3^1) \% 7. \\ \text{BP}_6 &= (\text{EP}_1^0 * \text{EP}_5^1 + \text{EP}_2^0 * \text{EP}_4^1) \% 7. \\ \text{BP}_7 &= (\text{EP}_2^0 * \text{EP}_5^1) \% 7 = 1. \end{aligned}$$

Now the given basic monic polynomial is,

$$\text{BP}(x) = \text{BP}_7 x^7 + \text{BP}_6 x^6 + \text{BP}_5 x^5 + \text{BP}_4 x^4 + \text{BP}_3 x^3 + \text{BP}_2 x^2 + \text{BP}_1 x^1 + \text{BP}_0 x^0.$$

$$\text{Decm_eqv}(\text{BP}(x)) = \text{BP}_7 * 7^7 + \text{BP}_6 * 7^6 + \text{BP}_5 * 7^5 + \text{BP}_4 * 7^4 + \text{BP}_3 * 7^3 + \text{BP}_2 * 7^2 + \text{BP}_1 * 7^1 + \text{BP}_0 * 7^0.$$

Coefficients of each term in the 1st monic elemental polynomial EP⁰ where, d₁=3; are defined as EP₀⁰, EP₁⁰, EP₂⁰, EP₃⁰. Coefficients of each term in the 2nd monic elemental polynomial EP¹ where d₂=4; are defined as EP₀¹, EP₁¹, EP₂¹, EP₃¹, EP₄¹. The value in suffix also gives the degree of the term of the monic elemental polynomials. Now, the algebraic method is as follows,

3rd block:

$$\begin{aligned} \text{BP}_0 &= (\text{EP}_0^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_1 &= (\text{EP}_0^0 * \text{EP}_1^1 + \text{EP}_1^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_2 &= (\text{EP}_0^0 * \text{EP}_2^1 + \text{EP}_1^0 * \text{EP}_1^1 + \text{EP}_2^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_3 &= (\text{EP}_0^0 * \text{EP}_3^1 + \text{EP}_1^0 * \text{EP}_2^1 + \text{EP}_2^0 * \text{EP}_1^1 + \text{EP}_3^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_4 &= (\text{EP}_0^0 * \text{EP}_4^1 + \text{EP}_1^0 * \text{EP}_3^1 + \text{EP}_2^0 * \text{EP}_2^1 + \text{EP}_3^0 * \text{EP}_1^1 + \text{EP}_4^0 * \text{EP}_0^1) \% 7. \\ \text{BP}_5 &= (\text{EP}_1^0 * \text{EP}_4^1 + \text{EP}_2^0 * \text{EP}_3^1 + \text{EP}_3^0 * \text{EP}_2^1) \% 7. \\ \text{BP}_6 &= (\text{EP}_2^0 * \text{EP}_4^1 + \text{EP}_3^0 * \text{EP}_3^1) \% 7. \\ \text{BP}_7 &= (\text{EP}_3^0 * \text{EP}_4^1) \% 7 = 1. \end{aligned}$$

Now the given basic monic polynomial is,

$$BP(x) = BP_7x^7 + BP_6x^6 + BP_5x^5 + BP_4x^4 + BP_3x^3 + BP_2x^2 + BP_1x^1 + BP_0x^0.$$

$$\text{Decm_eqv}(BP(x)) = BP_7 \cdot 7^7 + BP_6 \cdot 7^6 + BP_5 \cdot 7^5 + BP_4 \cdot 7^4 + BP_3 \cdot 7^3 + BP_2 \cdot 7^2 + BP_1 \cdot 7^1 + BP_0 \cdot 7^0.$$

In this way the decimal equivalents of all the monic basic polynomials or monic reducible polynomials are pointed out. The polynomials belonging to the list of reducible polynomials are cancelled leaving behind the irreducible polynomials. Non-monic irreducible polynomials are computed by multiplying a monic irreducible polynomial by α where $\alpha \in GF(p)$ and assumes values from 2 to 6.

2.2 General Algebraic method to find Irreducible Polynomials over Galois Field $GF(p^q)$.

Here the interest is to find the monic irreducible polynomials over Galois Field $GF(p^q)$, where p is the prime field and q is the extension of the field. Since the indices of multiplicand and multiplier are added to obtain the product. The extension q can be demonstrated as a sum of two integers, d_1 and d_2 . The degree of highest degree term present in elemental polynomials of $GF(p^q)$ is $(q-1)$ to 1, since the polynomials with highest degree of term 0, are constant polynomials and they do not play any significant role here, so they are neglected. Hence the two set of monic elemental polynomials for which the multiplication is a monic basic polynomial, have the degree of highest degree terms d_1, d_2 where, $d_1=1,2,3,\dots,(q/2-1)$, and the corresponding values of d_2 are, $(q-1), (q-2), (q-3),\dots,q-(q/2-1)$. Number of coefficients in the monic basic polynomial $BP = (q+1)$; they are defined as $BP_0, BP_1, BP_2, BP_3, BP_4, BP_5, BP_6, BP_7, \dots, BP_q$, the value of the suffix also indicates the degree of the term of the monic basic polynomial. For monic polynomials $BP_q = 1$.

Coefficients of each term in the 1st monic elemental polynomial EP^0 , where, $d_1=1,2,\dots,(q/2-1)$; are defined as $EP_0^0, EP_1^0, \dots, EP_{(q/2-1)}^0$. Coefficients of each term in the 2nd monic elemental polynomial EP^1 where $d_2= (q-1), (q-2), (q-3),\dots,q-(q/2-1)$; are defined as $EP_0^1, EP_1^1, EP_2^1, EP_3^1, EP_4^1, \dots, EP_{q-(q/2-1)}^1$. The value in suffix also gives the degree of the term of the monic elemental polynomials. Total number of blocks is the number of integers in d_1 or d_2 , i.e. $(q/2-1)$ for this example.

Now, the algebraic method for $(q/2-1)^{\text{th}}$ block is as follows,

$(q/2-1)^{\text{th}}$ block:

$$BP_0 = (EP_0^0 * EP_0^1) \% p.$$

$$BP_1 = (EP_0^0 * EP_1^1 + EP_1^0 * EP_0^1) \% p.$$

$$BP_2 = (EP_0^0 * EP_2^1 + EP_1^0 * EP_1^1 + EP_2^0 * EP_0^1) \% p.$$

$$BP_3 = (EP_0^0 * EP_3^1 + EP_1^0 * EP_2^1 + EP_2^0 * EP_1^1 + EP_3^0 * EP_0^1) \% p.$$

.....

$$BP_{q-1} = (EP_0^0 * EP_{(q-1)}^1 + EP_1^0 * EP_{(q-2)}^1 + \dots + EP_{(q/2-1)}^0 * EP_{(q-1)-(q/2-1)}^1) \% p.$$

$$BP_q = (EP_{(q/2-1)}^0 * EP_{q-(q/2-1)}^1) \% p.$$

Now the given basic monic polynomial is,

$$BP(x) = BP_q x^q + BP_{q-1} x^{q-1} + \dots + BP_5 x^5 + BP_4 x^4 + BP_3 x^3 + BP_2 x^2 + BP_1 x^1 + BP_0 x^0.$$

$$\text{Decm_eqv}(BP(x)) = BP_q \cdot p^q + BP_{q-1} \cdot p^{q-1} + \dots + BP_5 \cdot p^5 + BP_4 \cdot p^4 + BP_3 \cdot p^3 + BP_2 \cdot p^2 + BP_1 \cdot p^1 + BP_0 \cdot p^0.$$

Similarly all the decimal equivalents of all the resultant basic polynomials or reducible polynomials for all a and its corresponding b values are calculated. The polynomials belonging to the list of reducible polynomials are cancelled leaving behind the irreducible polynomials. Non-monic irreducible polynomials are computed by multiplying a monic irreducible polynomial by α where $\alpha \in GF(p)$ and assumes values from 2 to $(p-1)$.

2.3 General Method to develop each block of the Algorithm of the New Algebraic Method.

Prime field: p

Extension of the field: q .

$d_1=1,2,3,\dots,(q/2-1)$.

$d_2=(q-1), (q-2), (q-3),\dots,q-(q/2-1)$.

4. Conclusion.

To the best knowledge of the present authors, there is no mention of a paper in which the composite polynomial method is translated into an algorithm and turn into a computer program. The new algebraic method is a much simpler method similar to composite polynomial method to find monic irreducible polynomials over Galois Field $GF(p^q)$. It is able to determine decimal equivalents of the monic irreducible polynomials over Galois Field with a larger value of prime, also with large extensions. So this method can reduce the complexity to find monic Irreducible Polynomials over Galois Field with large value of prime and also with large extensions of the prime field. So this would help the crypto community to build S-Boxes or ciphers using irreducible polynomials over Galois Fields with a large value of prime, also with the large extensions of the prime field.

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Appendix

A sample list of Decimal Equivalents of Monic Irreducible Polynomials over Galois Field GF(7⁷) is given below.

823586	823587	823588	823589	823590	823591	823595	823596	823598	823601	823602
823604	823607	823611	823612	823614	823618	823619	823622	823623	823625	823630
823631	823633	823635	823636	823638	823643	823644	823646	823649	823653	823654
823658	823659	823661	823665	823666	823668	823670	823674	823675	823678	823679
823681	823684	823685	823687	823691	823692	823696	823698	823700	823701	823706
823708	823709	823713	823715	823716	823719	823721	823722	823726	823727	823731
823735	823737	823738	823740	823744	823745	823749	823750	823752	823755	823756
823758	823762	823763	823765	823770	823771	823773	823775	823779	823780	823782
823783	823785	823790	823792	823793	823796	823797	823801	823803	823805	823806
823810	823812	823813	823817	823818	823822	823825	823827	823828	823833	823835
823836	823838	823840	823841	823846	823848	823849	823852	823853	823857	823859
823860	823864	823867	823869	823870	823873	823875	823876	823882	823884	823885
823887	823892	823894	823899	823902	823905	823908	823913	823916	823919	823923
823926	823930	823931	823932	823933	823937	823940	823946	823948	823950	823954
823959	823962	823964	823965	823966	823967	823973	823975	823978	823980	823988
823990	823994	823997	824001	824003	824007	824010	824013	824017	824020	824021
824022	824023	824027	824029	824034	824037	824042	824045	824050	824051	824052
824053	824055	824057	824063	824065	824070	824074	824079	824081	824085	824088
824091	824094	824097	824098	824099	824100	824107	824109	824113	824115	824118
824122	824125	824127	824132	824134	824139	824142	824147	824149	824154	824157
824161	824165	824169	824170	824171	824172	824177	824179	824182	824185	824188
824190	824196	824200	824202	824205	824211	824212	824213	824214	824217	824219
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